

Notating Disfluencies and Temporal Deviations in Music and Arrhythmia

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Abstract

Expressive music performance and cardiac arrhythmia can be viewed as deformations of, or deviations from, an underlying pulse stream. We propose that the results of these pulse displacements can be treated as actual rhythms and represented accurately via a literal application of common music notation, which encodes proportional relations amongst duration categories, and figural and metric groupings. We apply the theory to recorded music containing extreme timing deviations and to electrocardiographic (ECG) recordings of cardiac arrhythmias. The rhythm transcriptions are based on rigorous computer-assisted quantitative measurements of onset timings and durations. The root-mean-square error ranges for the rhythm transcriptions were (19.1, 87.4) ms for the music samples and (24.8, 53.0) ms for the arrhythmia examples. For the performed music, the representation makes concrete the gap between the score and performance. For the arrhythmia ECGs, the transcriptions show rhythmic patterns evolving through time, progressions which are obscured by predominant individual beat morphology- and frequency-based representations. To make tangible the similarities between cardiac and music rhythms, we match the heart rhythms to music with similar rhythms to form assemblage pieces. The use of music notation leads to representations that enable formal comparisons and automated as well as human readable analysis of the time structures of performed music and of arrhythmia ECG sequences beyond what is currently possible.

Keywords

music representation, expressive music performance, cardiac arrhythmia, atrial fibrillation, irregular pulse, timing, meter, free rhythms, music notation

Introduction

Expressive music performance and cardiac arrhythmia share many common traits. An important one is that each can be viewed as the result of deviations from, or deformations of, an underlying pulse. Their origins suggest that the rhythms of such data streams can be encoded effectively using common music notation. We propose to treat these time displacements as bona fide rhythms and to represent them via a literal application of music notation. Music notation encodes abstract concepts of proportional relations amongst duration categories, and higher-level organising constructs such as figural and metric groupings, and is typically used for abstract or conceptual, rather than literal, representations of time. The literal application (and consequent reading) of common music notation is counter to its common use by composers or performers. It co-opts the existing notation system to create symbolic representations that can enable formal comparisons and computer and human (readable) analysis of time sequences.

This work was inspired by a transcription of sight-reading wherein the rhythm notation captured both musical and cognitive disfluencies. The transcription, created by ear with the aid of the original score and audio and MIDI recordings, demonstrated the possibility of notating serendipitous rhythms. In the current paper, we will use computer tools to rigorously mark onset times and obtain quantitative measurements of durations. The tempi and quantizations are chosen to maximize transcription

precision, and the accuracies of the rhythm transcriptions are evaluated quantitatively against the original timings. Figural and metric groupings and any metric modulations are chosen manually, although this too can be automated, as will be discussed.

The technique is first illustrated using contrasting music examples that contain extreme timing deviations introduced in performance. The results highlight the gap between the score and performance, made all the more obvious by the use of the same notation to communicate the difference between the rhythms. Next, we apply the same transcription process to electrocardiographic (ECG) recordings of cardiac arrhythmias. While such rhythm transcription can be applied to any arrhythmia, we demonstrate the method on three excerpts of ECG recordings of atrial fibrillation (AF). The notation shows clearly the rhythmic groupings and patterns such as repetitions and transformations through time. These are patterns normally obscured in the predominant ECG analysis approaches which mainly consider individual beat morphology or features aggregated over windows of time.

Similarities between cardiac and music rhythms are further made tangible by matching the heart rhythms to music with similar rhythms to form musical assemblages. We apply the notation and retrieval-and-assemblage process to the AF ECG recordings, leveraging the innate rhythmic

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similarities to music with mixed meters, a siciliane, and a tango to generate the mirror pieces.

The precise and symbolic representation of performers' idiosyncratic timings and of AF's capricious rhythms points to a host of new computational analysis approaches for characterizing and comparing such time sequences. Once a formal representation for time structure exists in symbolic form, any number of encoding schemes can be employed to transform the symbols to machine-readable formats. These encoding schemes facilitate fast searches for specific rhythms and repeated patterns, allow for data summarization and comparisons between sequences. Further analyses of the transcribed rhythms could reveal hierarchical structure in the time series data. Quantitative techniques can be devised to measure the distance, for example, between transcriptions of different performances of the same work. Finally, the symbolic representation lends itself to large-scale pattern search and categorization, for inferring performance style, characterising arrhythmia subtypes, or predicting diagnostic outcomes.

The remainder of the paper is organised as follows: first we review some related work on transcription, music performance, and mappings of cardiac information to music; next, we briefly review the sight-reading transcription that inspired this work; then, we present the transcriptions of the three performed music cases, followed by the three arrhythmia ECG transcriptions, and conclusions and discussions. An appendix documents the evaluations of the various transcriptions.

Transcription

The practice of transcription has an illustrious history. [Olivier Messiaen \(1956\)](#)'s use of birdsong in his compositions such as *Oiseaux Exotique*, *Vingt Regards*, and others is well known. The tradition of transcribing birdsong pre-dates Messiaen by many centuries. [Hold \(1970\)](#) gives a detailed account of composers' and naturalists' attempts at music representations of birdsong from 1240 onwards—these include staff, orthochronic, and graph notation, and the sound spectrograph.

Transcription has been especially useful for the study and reproduction of extemporaneous performances. Early examples can be found in [Vaclav Pichl's](#) transcriptions of [Luigi Marchesi \(1792\)](#)'s elaborate note embellishments in four performances of the aria "Cara negl'occhi tuoi" and the rondo "Mi dà consiglio" in [Nicola Antonio Zingarelli's](#) opera *Pirro ré d'Epiro*, as described in [Berger \(2016\)](#). The [Charlie Parker Omnibook \(1978\)](#), a collection of transcriptions of the jazz saxophonist's compositions and improvised solos, remains a staple in jazz studies. Historic performances like [Keith Jarrett \(1991\)](#)'s Köln Concert have been painstakingly notated for re-performance. Other transcriptions include [Coltrane \(1999\)](#), [Duke Ellington \(1971\)](#), [Bill Evans \(1967\)](#), and [Ferdinand 'Jelly Roll' Morton \(1986\)](#), as reviewed in [Tucker \(1982\)](#).

Ethnomusicologists and composers transcribe field recordings of folksongs for analysis and as seed material for new compositions, respectively. [Bela Bartok \(1942\)](#) carefully converted to music notation the melodies of recorded songs in the Milman Parry Collection for re-use in compositions, see discussion in [Frigyesi \(1985\)](#).

More recently, the push towards empirical study of vernacular music has led to the transcription of traditional Chinese clapper and rap music for systematic analysis; see [Sborgi Lawson \(2012\)](#) and [Ohriner \(2016\)](#), respectively.

This work was motivated in part by [Grønli, Child, Chew \(2013\)](#)'s "Practicing Haydn", in which a sight-reading of a Haydn sonata movement is transformed into a performable score via transcription, complete with all the repetitions, pauses, starts, and stops. The transcription of sight-reading raises the following question: If the blundering mishaps and accidental discontinuities of a first encounter with a score can be recorded using music notation, what else might be amenable to such treatment? Here, we show that expressive performance and arrhythmia sequences can also be subject to such transcription processes, although the goal is not to produce a performable score, even though that is a desirable side effect, and the transcription will use a computer-assisted process that aims to minimise discrepancies between original and transcribed sequences.

Related to transcription of expressive performance, there exists a long tradition of scholarly work on the representation of intonation, dynamics, and pacing in expressive speech dating back to [Steele \(1775\)](#). Recent forays into the transcription of speech melody and timing have turned to the direct use of music notation in a literal fashion. Leveraging commonalities between expressive speech and music, [Simoes and Meireles \(2016\)](#) and [Meireles et al. \(2017\)](#) explored the use of music notation to represent the melody and rhythms of spoken language. In this work, the transcriptions are treated as literal expressions of the spoken pitches and durations. They are uniformly presented in 4/4 time, without regard to meter, although the authors propose to obtain natural metrical groupings from the stresses in speech in future work.

The current paper applies music transcription to unconventional contexts of expressive performance and cardiac arrhythmia, with the goal of recording these temporal processes and experiences, which are not normally preserved in writing. Special attention will be given to precise representation of timing and durations, and to the figural and metrical groupings that may be inferred from the patterns.

Representing Performed Music

The first application addresses the representation of performed music. The increased emphasis on music as performance rather than music as writing or notation combined with the growth of computer tools for analysis of performed music brings to a head issues of representing performed music. Anyone who has tried to generate a sound file from a digital score soon discovers that a performance rendered from the digital score is vastly different from that realised in practice. Thus the information encoded in the score is insufficient for creating or re-creating a convincing rendition of the music. This is because, as [Frigyesi \(1993, p.60-62\)](#) points out, notation was not conceived to be transcription; it represents only an abstraction of the temporal experience, and not the actual rhythms of a performance. It is worth noting that the view of transcription as literal and notation as abstract is not universal. For example, [Busoni](#) considers the transfer of a piece from one instrument to another, the transfer of music concept to

notation (composition), and from notation to performance to be different forms of transcription, see [Knyt \(2010, p.111\)](#). The transcriptions in this paper will use notation literally to encode time and other structures.

Music as performed differs from the information denoted on the page for many reasons. In performed speech, the measure of syllables and words in a text fall far short of the timings of the delivery. In music playing that aspires to the rhetorical style of spoken language à la Adolph Kullak, see [Cook \(2013, p.74\)](#), performed rhythms privilege the cadences and pacing of speech over the music script. Due to the relative nature of loudness and other constraints, notated dynamics are also frequently not what they seem: [Kosta, Bandtlow, Chew \(2014\)](#) showed that notes marked *pianissimo* can sound objectively louder than notes marked *fortissimo*, depending on context. Furthermore, music performance practice often requires that performers deviate from the written score in prescribed ways. For example, in the French tradition of notes inégales, notes of equal duration are deliberately lengthened or shortened in performance, see [Houle \(2000, p.86\)](#). In many folk traditions, notated pitches may be lavishly ornamented in practice, as shown in [Yang, Chew, Rajab \(2013\)](#)'s study comparing erhu and violin performances of a Chinese folk piece.

But, what if actual performed rhythms were transcribed literally and precisely using conventional notation so as to make the nuances of performance concrete through writing? The encoding would still be incomplete as the symbolic representation would not capture fine details such as the exact shapes of note articulations, transitions, and within-note embellishments. Some degree of approximation of the precise timings will be inevitable to ensure the readability of the transcription; even if the transcription could provide notation to millisecond precision, there are limits to what the human ear can distinguish as two separate time instants, see [Bartlette et al. \(2006\)](#), [Chafe, Caceres, Gurevich \(2010\)](#) and [Chew et al. \(2004\)](#). Nonetheless, a faithful transcription would give a much more accurate (literal) representation of the temporal experience, and would allow for direct comparison with the original score as a measure of the distance between the abstract representation and actual experience.

Notation of and for performance have taken many forms. [Philip \(1992\)](#) has explored the notation of nuances in expressive timing in less quantitative ways. Moving away from conventional music notation, [Bamberger \(2000\)](#)'s Impromptu software uses multiple representations such as pitch contours, rhythm bars, and piano roll notation to allow users to manipulate properties of tune blocks. Many other graphical notations exist, including [Farbood \(2004\)](#) and [Hope and Vickery \(2015\)](#). As an intermediary between conventional notation and digital sound, [Bresson and Assayag \(2011\)](#)'s OpenMusic, a programming environment designed for composition and analysis, allows notes to be positioned on staff lines in continuous locations indicating the times at which they sound, with impact on the readability of the score. A goal here will be to explore the limits of using conventional music notation to represent continuous time, bearing in mind that not all locations on the continuous time axis are equally likely given the pulse-based origin of the input.

The first set of examples takes on this challenge to transcribe the actual timings of recorded expressive performances. In so doing, it provides in a sense a written record of the performers' creative work. The three cases span music from a variety of Western music traditions: the Vienna Philharmonic Orchestra's performances of Johann Strauss II's "The Blue Danube", a traditional New Year's concert encore piece; Maria Callas' rendition of Giacomo Puccini's operatic aria "O Mio Babbino Caro", and Marilyn Monroe's sultry rendition of "Happy Birthday" on the occasion of John F. Kennedy's 45th birthday.

The body of scientific research on performance practice has expanded rapidly, aided by recent software tools such as Sonic Visualiser by [Cannam, Landone and Sandler \(2010\)](#). It is now possible for any motivated person with modest computer literacy to be able to extract beat and loudness information from a recorded performance. Because of the visual and compact nature of information portrayed on graphs, the scientific study of music performance and music expression predominantly use graphs of timing, tempo, and/or loudness data extracted from audio recordings—see, for example, [Todd \(1992\)](#), [Cheng and Chew \(2008\)](#), and [Chew \(2016\)](#). There has scarcely been any attempt to notate these captured rhythms due partly to the gulf between event-based (notation) and signal-based (audio) representations, and partly to the difficulty of representing free rhythms, which will be discussed in upcoming paragraphs.

An exception can be found in the work of Beaudoin and Senn, described in [Beaudoin \(2012\)](#), in which the exact timings and intensity levels of Martha Argerich's recording of Chopin's "Prelude in E minor", Op. 28/4, is transcribed to standard notation as the framework for a series of pieces based on transformations on Chopin's original material called *Études d'un Prélude*. Another is the work of [Grønli, Child, Chew \(2013\)](#) in which Chew's sight reading of the finale movement of Haydn's *Piano Sonata in E♭*, Hob XVI:45 is meticulously transcribed by Child for re-performance. The resulting composition, "Practicing Haydn", was created for and premiered at Grønli's solo art show at the grand opening of the Kunsthall Stavanger, and at other venues.

Musica Humana

The second application lies in the domain of cardiac arrhythmia. The belief that music was inherent in the beating of the pulse was widely held in the middle ages. This was a specific instance of the more general idea that music was inherent in the rhythms of the human body—Boethius' *musica humana*, which is complementary to *musica instrumentalis* (music of sounding instruments) and *musica universalis* (music of the spheres), see [Chamberlain \(1970\)](#). [Siraisi \(1975\)](#) provides a rich survey of academic physicians' detailed writings on the nature of the music of pulse in the 14th and 15th centuries. Since then, arts and medicine have diverged and developed along separate paths. Today, with the parallel development of annotation and visualization tools like WFDB by [Silva and Moody \(2014\)](#) and LightWAVE by [Moody \(2013\)](#) for ECG data, there is ample evidence that the human pulse would be amenable to modern musical treatment and analysis as the fields are poised to collide again.

As a step towards facilitating this re-connection, the second set of examples applies transcription to represent, using conventional music notation, the rhythms of arrhythmia. Music representation of cardiac information is not new, although it has been used primarily to describe heart sounds. René Laennec (1826), the inventor of the stethoscope, used mainly onomatopoeic words to depict sounds he heard in the process of auscultation; however, on one occasion in 1824, he resorted to music notation to augment his word description of a venous hum. Segall (1962) points to this as the first symbolic representation of the sound of a heart murmur, with many more graphical notations to follow. More recently, Field (2010) used music notation to systematically transcribe signature heart sounds and murmur patterns in the teaching of cardiac auscultation to medical students to aid the diagnosis of heart valve disorders.

We will also use music notation to represent heart rhythms, but now focusing on transcribing recorded rhythmic sequences of abnormal electrical activity in the heart. Conditions resulting from abnormal electrical conduction differ from those due to valvular disorders; the input will also be the ECG trace instead of sound.

Conventional ways to represent ECG data tend to focus on individual beats: their morphology (features of the waveform) or categorical labels such as N (normal) and V (ventricular activity); or, frequency domain characteristics like heart rate variability that aggregate features over larger windows of time. Counter to this trend, Bettermann et al. (1999) used a binary symbol sequence from African music theory to represent elementary rhythm patterns in heart period tachograms. Syed et al. (2010) considers motivic patterns based on short strings of the categorical labels, and Qiu et al. (2016) has studied the semantic structure of symbols labelling parts of the waveform.

In the context of the transcription exercise, the notated rhythms are next matched to existing music with similar rhythms, and new compositions generated by collaging together appropriate parts of the selected piece. Since the chosen music already has the same or a very similar rhythmic structure, the collage gives pitch to the rhythms in ways that reinforce and make more readily perceptible the inherent time structures. If the pitch structures are in dialogue with the time structures, it can add a layer of complementary structures. In either case, the temporal experience of arrhythmia can be made visceral through the performance of the resulting music.

Composing with rhythm templates is not new. Composer Cheryl Frances-Hoad's piano piece "Stolen Rhythm" (2009) takes the notated rhythms of the finale movement in Haydn's Piano Sonata in E \flat , Hob XVI:45, and assigns new notes to them. The computer program MorpheuS also takes rhythms from existing pieces and sets new notes to them in ways that preserve the repetitions patterns and tonal tension profiles of the template piece, see Herremans and Chew (2017). "Practicing Haydn" in effect creates a collage by traversing Haydn's piece through a series of repetitions and pauses.

Heartbeat data has been used as a source for music composition or synthesis. The most common approach is to use heart rate variability indices, which are based on statistical aggregation over longer time spans. They also tend towards direct data sonification. In the Heartsongs

CD by Davids (1995), produced as part of ReyLab's Heartsongs Project, heartbeat intervals were averaged over 300 beats to remove local fluctuations and mapped to 18 notes on a diatonic scale to create the melody. Yokohama (2002) maps each heartbeat interval to Musical Instrument Digital Interface notes, so that an intervallic change such as a premature beat triggers a more significant change in pitch. In Ballora et al. (2006), heart rate variability data is mapped to pitch, timbre, and pulses over a course of hours for medical diagnosis; in Orzessek and Falkner (2006), heartbeat intervals are passed through a bandpass filter and mapped to MIDI note onsets, pitch, and/or loudness. Votava and Berger (2011)'s Heart Chamber Orchestra uses interpretations of its 12 musicians' heartbeats, detected through ECG monitors, and relationships between them influence a real-time score that is then read and performed by the musicians from a computer screen. All but one of these studies—Yokohama (2002)—have focused on heartbeat data from non-arrhythmic hearts.

In this paper, transcription serves as a means to represent the rhythms of arrhythmia using conventional music notation. Current analyses of ECG data predominantly use beat morphology- and frequency domain-based representations. The music notation captures local rhythmic patterns that are lost in single-beat and frequency-based approaches. Three different excerpts, short summaries, showing a heart in different states of atrial fibrillation (AF) are chosen from a continuous 18-hour recording from a 3-lead Holter monitor. The rhythms of the different states of the arrhythmia are made apparent in the extracted musical rhythms and collage pieces.

Transcription Process

Conventional music notation is the representation of choice for the transcriptions in this paper. The examples addressed in this paper tend towards the practice of free rhythm, which is common in both folk and art, religious and secular traditions. Free rhythm is "the rhythm of music without pulse-based periodic organization" Clayton (1996, p.329). The analysis of free rhythm music remains an open challenge, with a major hurdle being the difficulty of representing free rhythms in writing. Existing efforts to notate free rhythms typically avoid time signatures or barline, sometimes simply arranging note heads on a horizontal time line so as to avoid the implications of pulse or meter in staff notation.

The reason regular staff notation is adopted here is that the examples are all pulse based; this includes both the performed music as well as the cardiac arrhythmia time series. While they generally lack periodic structure and do not possess ordinary metrical organization, due to pauses and pattern repetitions, local grouping structures do exist, which allow for the assignment of changing time signatures and indications of figural groupings through phrase markings. In line with notations used in contemporary compositions, the transcription of "Practicing Haydn", and indeed those for the performed durations and arrhythmia sequences make copious use of changing meters (like in Stravinsky's compositions), and metric modulations (like in Elliot Carter's works).

A main objective in the transcription process is to minimize the difference between the recorded and the transcribed sequence. When a design goal is to minimise transcription error, there exists the possibility to make the notation enormously complex to achieve the highest possible accuracy. To counter this, an important and competing aim is to ensure that the proportional durations in the notation are readily readable by human eyes so that it could serve as a source for visual analysis or performance. In this way, the notation is suitable both as input for computer analysis as well as for visual inspection. Metric modulations are kept to a minimum, and utilized only when they lead to simpler proportional durations. To satisfy the second goal, when a human performer plays the notated transcription, it should be possible to reproduce the original rhythms without the aid of a click track like in <https://vimeo.com/226516952>, although clearly it would be easy to choose to deviate significantly from the score. Thus, the labyrinthine density of notation like that employed by Brian Ferneyhough as a conduit for his complex composition process are avoided in favor of simpler forms. In the case of Ferneyhough's intricate notations, designed to serve the purpose of lifting players beyond hackneyed readings of the score, some such as Marsh (1994) have argued for simpler representations that directly reflect specific interpretations of the music. Distinct from Marsh's goals, even though a secondary constraint of the transcription process here is human readability, the transcriptions do tend to make the score more complex in order to incorporate recorded nuances. Here, metric modulations that use irrational proportions, as in Conlon Nancarrow's "Study 33", are strictly avoided. One might argue that even Nancarrow's irrational proportions can be closely approximated using conventional notation (rational durations) for playability, see Callender (2014).

Rhythmic Disfluencies

The transcription of performed rhythms and the rhythms of cardiac arrhythmias draws inspiration from "Practicing Haydn" by Chew, Child and Grønli (2013). "Practicing Haydn" originated as an idea by Grønli and Child to create a musical piece that sounds like musicians warming up and practicing before a concert. The result was a transcription of the serendipitous rhythms of a sight-reading of a Haydn sonata movement for re-performance, complete with all the repetitions, starts, and stops. The première of the piece took place concurrently at the grand opening of the Kunsthall Stavanger in Norway by Chew and at Performa13 in New York City by pianist Elaine Kang—see videos at <https://kunsthallstavanger.no/en/exhibitions/practicing-haydn>.

Three selections from the transcription are given in Figures 1 through 3. Each figure shows a snippet from the original Haydn score and from Child's transcription of Chew's sight-reading of the corresponding bars. The transcribed segments are inevitably longer than the original score due to repetitions, and to pauses and hesitations.

An interesting side effect of the exercise is that the transcription serves as a record of not only the musical but also the cognitive disfluencies. Unexpected events provide moments for pause. The transcribed sight-reading in



(a) bars 40 – 41 from Haydn's sonata movement



(b) Chew's sight-reading of the excerpt

Figure 1. Chew's sight reading of Haydn's Piano Sonata in E \flat , Hob XVI:45 finale: pauses and repetitions.



(a) bars 44 – 45 from Haydn's sonata movement



(b) Chew's sight-reading of the excerpt

Figure 2. Chew's sight reading of Haydn's Piano Sonata in E \flat , Hob XVI:45 finale: slow-downs, repetitions, and hesitations.

Figure 1b shows a pause at the end of the second bar just before an unfamiliar turn in the 16-th note sequence; the excerpt in Figure 2b documents the hesitations just before the introduction of figural or directional changes; the pickup into the 2/4 bar re-starts an unexpected figure that was not fully apprehended on the first play in the preceding 3/8 bar; a similar re-start can be observed in Figure 3b. Repetitions help refine harmonic direction: in Figure 1b the trill is repeated to reinforce its harmonic function; in Figure 2b, the final tonic chord is elongated to balance the length (and emphasis) of the preceding dominant chord.



(a) bars 47 – 49 from a Haydn sonata movement



(b) Chew's sight-reading of the excerpt

Figure 3. Chew's sight reading of Haydn's Piano Sonata in E \flat , Hob XVI:45 finale: repetitions and wrong note.

That sight-reading is associated with hesitation and fumbling is not particularly remarkable. What is interesting here is that these behaviors are clearly documented in the transcriptions. They may be obvious to a casual listener, but the fact that they show up clearly in the transcriptions means that it is possible to automate the detection process to enable large-scale analysis of disfluent or rhythmically irregular behavior.

Choreographed Rhythms

When a score is interpreted by a human musician, the performed timings and durations are more often than not different, sometimes significantly so, from the notation in the score. Some of these deviations will be due to human inconsistency, but in skilled performance, the bulk of it can be ascribed to deliberate shaping of time, called *rubato*, either according to established convention or individual idiosyncrasy. In Cook (1987), rubato is encoded using note and bar durations, and percentage deviation from the norm. In Repp (1992), rubato in melodies, represented in eighth note durations (longer-duration notes are subdivided equally into eighth notes), are shown to frequently follow the shape of a quadratic curve. This method of representing tempo rubato persists to today and can be found, for example, in the work of Spiro, Rink and Gold (2016).

This section seeks to represent several different kinds of timing deviations in music performance. Curve fitting, where present, is done with the Matlab spline function and the precisely quantified durations transcribed to common music notation.

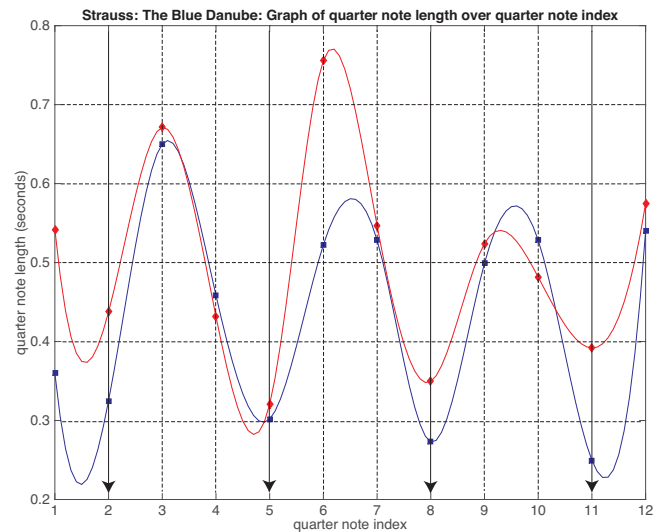
Viennese Waltz

The Viennese waltz is a prototypical example of music in which there is systematic disparity between notated and performed rhythms. The social context and bodily movements (steps and twirls) behind this dance form is explored in McKee (2011). For the musicians performing, the three beats of a Viennese waltz are typically played unequally, normally with the first beat shortest followed by the third, and with the second beat longest, although exceptions exist. Assuming a steady pulse, this could be interpreted as the second beat being early, a deviation from its prescribed onset time, giving the impression that the third beat is late due to the resulting larger gap between the second and third beats. Figure 4 shows, using graphs and music notation, how the notated and performed rhythms differ in Johann Strauss II's "The Blue Danube".

Figure 4a shows Strauss' original notated durations. To extract the performed durations from recorded performances, quarter note beat onset times (in seconds), $\{o_1, o_2, \dots, o_N\}$ where N is the total number of onsets, were annotated using Sonic Visualiser, Cannam, Landone and Sandler (2010), and checked aurally as well as visually using the audio waveform and spectral information. Beat durations are derived from these onset times, $d_i = o_{i+1} - o_i$, and graphed in Matlab; data interpolation was done using the Matlab spline function. Figure 4b shows the resulting graphs generated from performances of "The Blue Danube" by the Vienna Philharmonic with Herbert von Karajan (1987) and with Georges Prêtre (2010). These particular recordings were



(a) Strauss' notated durations



Performance by Vienna Philharmonic with Prêtre is marked by blue squares and with Karajan by red diamonds, respectively. Arrows mark the downbeat of each bar.

(b) Graph of performed durations (in score time)



(c) Transcription of Karajan's performed durations



(d) Transcription of Prêtre's performed durations

Figure 4. Excerpt from "The Blue Danube" by Johann Strauss II and analysis and transcription of recorded performances by the Viennese Philharmonic Orchestra conducted by Herbert von Karajan (1987) and by Georges Prêtre (2010).

chosen because they present two contrasting interpretations of "The Blue Danube", which show as divergences in the graphs and the rhythm transcriptions. These differences are all the more interesting because they were created by the same orchestra, albeit 23 years apart, performing under different conductors. In the plot, Figure 4b, arrows mark the downbeat of each bar. Note that if the music, the score shown in Figure 4a, was performed literally, exactly as notated, the plot would show only horizontal lines, indicating that all quarter notes have identical durations. This is clearly not the case as both lines show strong oscillations with varying amplitudes.

The transcription of the performed durations can be described in the form of a heuristic. Suppose the second beat is considered to be early, then the third beat is the

one that most closely resembles a full beat duration. Thus, we obtain the baseline beat duration from the third beat, which is assumed to be 2 or 3 eighth notes in length. The duration of the third beat served as the reference from which proportional relationships are derived for the preceding beats. Simple ratios—such as 3:2, 2.5:2, 1.5:2, and 2:3—were preferred over more complicated ones. Whether the third beat was 2 or 3 eighth notes in length is determined by which interpretation most closely approximated the simpler ratios. Suppose the e_i is the duration of the eighth note when the third beat is i eighth notes long, i.e. $e_i = d_{b_3}/i$ where b_j is the beat index of the j -th beat, d_{b_j} is the duration of the b_j -th beat, and n_{b_j} is the closest whole number or simple fraction when d_{b_j} is divided by e_i . Whether the third beat is 2 or 3 eighth notes long is determined by $\arg \min_{i=2,3} \sum_{j=1,2,3} \|d_{b_j}/e_i - n_{b_j}\|$. Note that this technique can be extended to consider other duration categories for the third beat such as 2.5 eighth notes.

After obtaining the duration ratios, the tempo for any contiguous set of beats, from i to j , is then computed from the total duration, $d = \sum_{k=i}^j d_k$, and total quantized score durations, $n = \sum_{k=i}^j n_k$, thus the tempo when a beat is two eighth notes long is given by $T = 30 \cdot n/d$ bpm. The resulting notation is shown in Figures 4c and 4d. The duration category for the third beat can also be chosen to keep the tempo as unchanging as possible from one bar to the next. For example, the third bar in Figure 4d could have been notated with {1.5, 3.5, 2.5} eighth note durations at basically the same tempo as the preceding bars. However, a metric modulation (change in tempo) gives a simpler notation that keeps the upbeat a quarter note. This simpler notation, which is more friendly to the human eye and requires only a subtle tempo slow down, is preferred.

Any rhythm transcription necessarily requires some degree of quantization. The original rhythms exist on the real time line, while the notation is categorical in nature. A transcription thus maps real numbers to duration categories. We are interested in the discrepancy between the real number and the categorical representation. We measure the accuracy of a transcription by the root-mean-square error (RMSE) between the transcribed inter-onset-intervals (IOIs) as compared to the IOIs in the recorded performances. If \hat{e}_i is the duration of the eighth note given by the tempo at the i -th beat, the RMSE is given by $\sqrt{\frac{1}{N} \sum_{i=1}^N (d_i - n_i \hat{e}_i)^2}$. For the examples shown in Figure 4, the RMSE is 19.1 ms for the Karajan excerpt and 24.9 ms for the Prêtre excerpt, respectively. The numbers are given in Table 1 and graphed in Figure 18 in the Appendix. The small errors show the very slight degree of approximation introduced in the transcription process.

The difference between the heuristic described here and a more conventional approach like transcribing the rhythms by ear is that the heuristic can be readily translated into a computer program to automate the transcription process. Manual transcription is possible and often desirable for small examples, but scalability is an important consideration for rhythm transcription to be deployable on a large scale for analysis. The method also has the advantage of providing rigorous control over and monitoring of the quantization error.

Many automatic or semi-automatic methods for rhythm transcription exist, see Ycart et al. (2016) and Nakamura, Yoshii and Sagayama (2017), as well as algorithms for supporting tempo detection Grosche and Mueller (2011) and tempo change Quinton (2017). However, frequency-based methods such as those described in Grosche and Mueller (2011) and Quinton (2017) still lack the reactivity required for the frequent meter changes needed to encode free rhythms. The state-of-the-art methods described and evaluated in Nakamura, Yoshii and Sagayama (2017) are designed to recover a score like the one originally written by the composer from the performance. They thus remove the temporal information that is inserted during performance. The work that comes closest to addressing the kind of transcription problem at hand is Ycart et al. (2016)'s interactive rhythm quantification (RQ) software, designed for use by composers as part of Open Music. At present, the software needs further optimization to make it comparable to human efficiency. The method above has the advantage of having been optimized for the special case of the Viennese waltz, which as it stands lacks generality. Adaptations tailored to other music styles will be described in the following sections.

In Figure 4, apart from knowing at a glance that the performances are not metronomic, the information embedded in a transcription gives not only the degree of variation, but also the metric modulations, proportional time relations, the precise timing of each note, the distribution of time across the pulses in each bar, and patterns of stress. Figure 4b shows Karajan's more steady (from bar to bar) Viennese waltz rhythm compared to Prêtre's more variable rhythm, which has the short-long gesture growing larger then shrinking. This observation is reinforced in the notation of Figures 4c and 4d. Karajan's performance could be captured with a constant 5/8 meter after the initial slow start; Prêtre's performance had to be notated with many more metric modulations—with the beat rate slowing to make the larger gestures that then compress to speed up—and proportional duration category changes. In both cases, the performed durations show marked, and notatable, differences from the original score. The notation thus records the ways in which the score itself is changed and re-shaped by the performer; this is made more obvious by the fact that the original composition and the performed rendition are encoded using the same notational conventions.

Operatic Aria

The performer has greatest latitude in creating free-sounding rhythms in solo performance. Amongst soloists, opera singers are well known for their flexible interpretation of notated rhythms. This second example examines the notation of extreme timing deviations or pulse elasticity in a solo performance of an operatic aria.

Figure 5 shows the duration of each eighth note in an excerpt of "O Mio Babbino Caro" from Giacomo Puccini's opera, *Gianni Schicchi*, when performed by Kathleen Battle, Maria Callas, and Kiri te Kanawa. The performed timings of these three recordings have been graphed and analysed in Chew (2016). The analysis is briefly described here before Callas' performance is singled out for transcription.

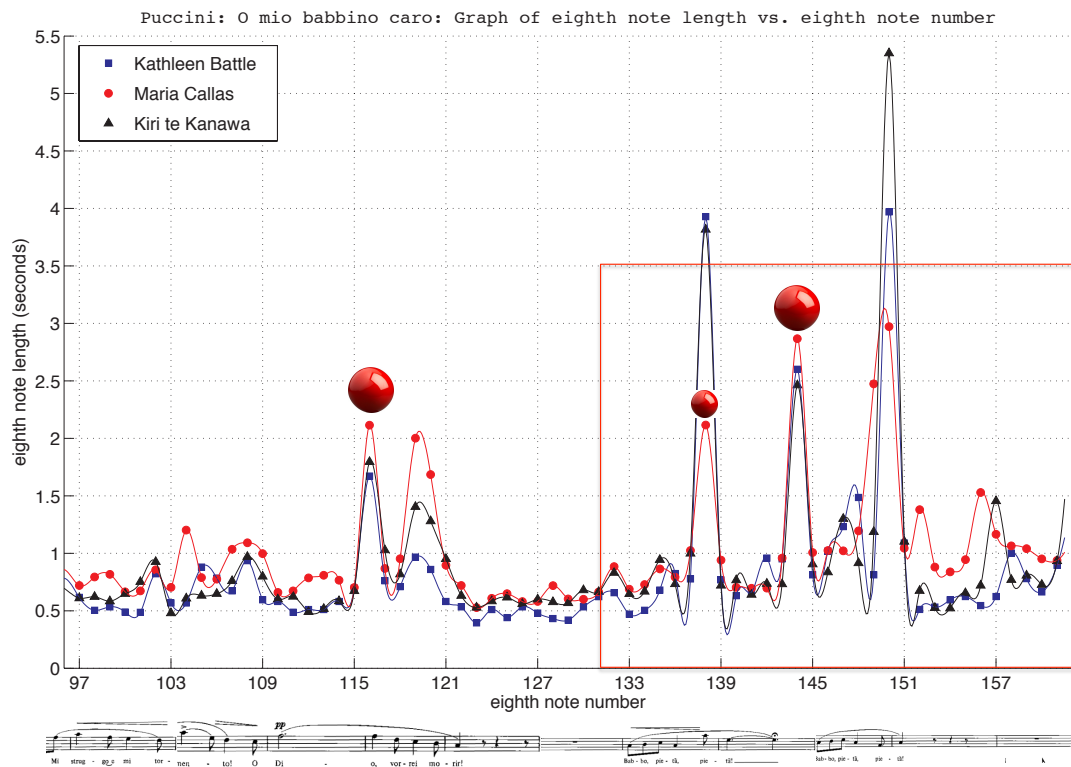


Figure 5. Eighth note durations in performances of an excerpt from Puccini’s “O Mio Babbino Caro” by Kathleen Battle, Maria Callas, and Kiri te Kanawa, with tipping points in Callas’ performance highlighted; the data is graphed in score time and vertical gridlines mark the first eighth note of each bar.

As before, the eighth note beat onsets were annotated and overlaid on the audio signal for inspection in Sonic Visualiser and evaluated aurally for correctness; the eighth note durations were then obtained from the annotated onsets. This was done for recordings by each of the three sopranos, and the durations plotted on the same graph. To allow for comparisons between the three recorded performances, the three sets of data were plotted in score time, i.e. with eighth note count as the x -axis. Again, interpolation between consecutive duration points was done using the Matlab spline function. The vertical dotted gridlines in the background mark the first eighth note of each bar. The corresponding solo melody is shown beneath the graph itself.

The first thing to note is the large degree of variation in eighth note durations over the course of even this short excerpt. The baseline eighth note duration hovers around 0.5 seconds, indicating that the underlying tempo is approximately 120 eighth notes per minute. In 6/8 time, with three eighth notes to a beat, this translates to a languid pulse of 40 beats per minute. The longest eighth note duration, corresponding to the highest point in Kiri te Kanawa’s plot, exceeds 5 seconds, extending almost to 5.5 seconds. This is a remarkable more than ten-fold increase from the baseline duration. It is such extreme timing deviations that challenge conductors and collaborative artists to virtuosic feats of prediction and adaptation.

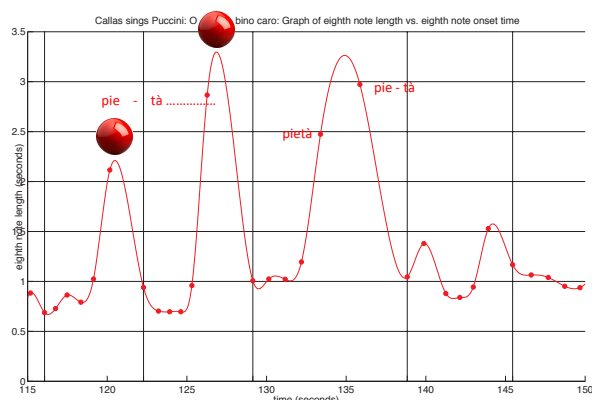
While there is a fair degree of commonality in where each performer chooses to invoke the most significant of these excursions from the underlying pulse grid, the ways in which they navigate these and other transitions form unique and often recognizable signatures of the performer or a performance. These time perturbations are the result of practiced choreography to influence the perceived musical context and impose structure on the musical text, to create emphases, and to elicit the desired emotion response from the listener. Such timing variations form the core evidence of the work behind each performance. Thus, it is helpful to be able to see this work represented concretely using an encoding familiar to any musically literate viewer.

In the special case where the stretched pulses coincide with the music structures to elicit a feeling of a roller coaster at the crest of a hill, they are called tipping points, see Chew (2016) or Chew (2017). In Figure 5, cue balls are perched atop each tipping point in Maria Callas’ performance. Not all extreme timing deviations are tipping points, and not all tipping points are signaled by a generous use of time. For an empirical study on what generates tipping points, see Naik and Chew (2017).

Figure 6 focuses on the excerpt within the rectangular box in Figure 5. Figure 6a shows the composer’s original notated durations. Figure 6b shows Maria Callas’ performed durations in performance (or real) time; listen to this excerpt at <https://vimeo.com/127507105>. Here,



(a) Puccini's notated durations



(b) Graph of Callas' performed durations (in real time)



(c) Notation of Callas' performed durations

Figure 6. Excerpt from “O Mio Babbino” by Giacomo Puccini and Maria Callas’ recorded performance.

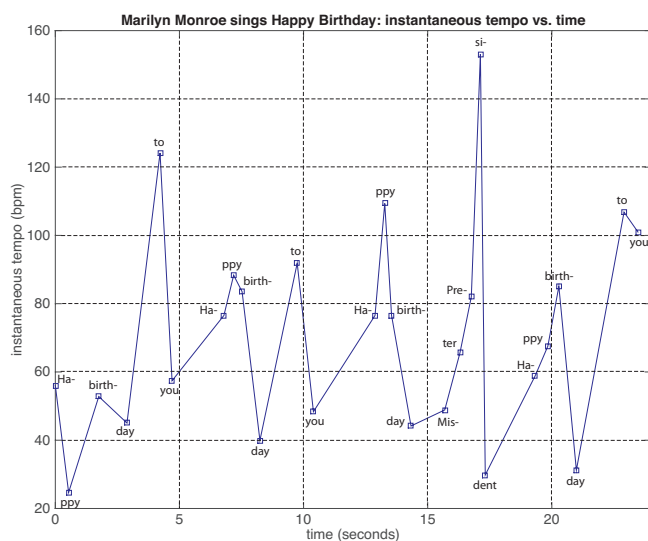
the durations of each eighth note are not plotted against an index of eighth note counts, but are plotted at the time at which they occur to allow for synchronization with the audio. For a discussion on score time vs. performance time, see [Chew and Callender \(2013\)](#). This plot is also interpolated using a spline function.

Figure 6c shows a transcription of Callas’ recorded performance. The transcription process is straightforward. Because the excerpt begins with a fairly steady (in performance) eighth note sequence, an underlying pulse grid can be established quickly for the proportional durations. On the repeat of the phrase, the durations of the three eighth notes sequence are longer. Hence, the notation was greatly simplified by invoking a metric modulation, from 86 eighth notes per minute to 60 eighth notes per minute, which provided a new unit pulse length rather than persisting with the same unit pulse. The RMSE between the performed and transcribed durations for the notes of the excerpt shown in Figure 6 is 87.4 ms; the precise details are shown in Table 2 and Figure 19 in the Appendix.

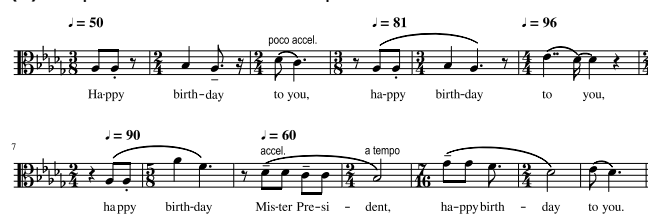
From both the graph as well as the transcription, it is clear that many notes are elongated beyond their notated durations for emphasis and expressive effect. Additional time has been inserted for breaths and to segment the phrases and sub-phrases. Musically, the first big elongation (the tipping point marked by the leftmost red cue ball in Figure 5) is part of a big *ritenuto* at the end of the first four bars, the second tipping point stretches the octave leap up to the A^b , and the third tipping point provides a pause (and breath) before



(a) Normal notated durations for “Happy Birthday”



(b) Graph of instantaneous tempi in Monroe's rendition



(c) Notation of Marilyn Monroe's performed durations

Figure 7. “Happy Birthday” as performed by Marilyn Monroe.

the final *ritardando* at the last two bars. Unlike conventional ways of marking these expressive gestures, such as by using labels like *ritenuto* and *ritardando*, the graph (Figure 6b) and notation (Figure 6c) show the details of exactly which eighth notes are lengthened, by how much, and which ones not. The notation additionally show the glissandi, marked by distinct note pairs connected by small slurs in the second and fifth bars in Figure 6b. As indicated by the metric modulation, the two sub-phrases are performed at different tempi's, with the second one a step slower than the first. Visual inspection of Figure 6c and Figure 6a makes apparent the marked difference between Callas’ performance and the score.

Happy Birthday

To show that the literal notation of expressive timing is not confined to classical singing, but also to vernacular forms, we turn our attention to [Marilyn Monroe \(1962\)](#)’s sultry rendition of “Happy Birthday” performed and recorded live in Madison Square on the occasion of the US President John F. Kennedy’s 45th birthday.

Figure 7a shows the conventional notation for the “Happy Birthday” melody. Figure 7b shows a graph of the instantaneous tempo at each syllable in Monroe’s performed rendition of the tune. For greatest precision, the onsets of every syllable was annotated using Sonic Visualiser and checked against the audio signal and spectrogram of the audio signal. Each “Happy” gave the approximate duration

of an eighth note and tempo for each new sub-phrase sometimes the tempo had to be changed at “to you” depending on the rate at which the words were sung. The RMSE between the performed and transcribed durations for the notes shown in Figure 7 is 51.5 ms; the details are shown in Table 3 and Figure 20 in the Appendix.

Because the syllables map to a variety of duration categories in the score, it is not straightforward to generate a graph of eighth note durations in score or real time. Instead, the instantaneous tempo is plotted in real time (as opposed to score time) at the instance of onset of each syllable. The instantaneous tempo at each syllable, T_s , is computed as a function of the onset times, $\{o_i\}$ (in seconds), and the corresponding syllable’s notated duration, $\{s_i\}$ (in beats), and is given by $T_s = 60 \cdot s_i / (o_{i+1} - o_i)$. Note that here, local minima signal the pauses or momentary slow downs, while the peaks mark the fastest sung syllables. Because Marilyn’s singing of “Happy Birthday” is almost speech-like in its flexible interpretation of time, the transcription led to the simplest notation when invoking multiple metric modulations, practically at every two-word sub-phrase.

The breathlessness of Marilyn’s singing is marked by the many pauses she takes, which show up as local minima in the plot in Figure 7b. The many pauses break the usual flow of the melody as well as the phrases in the text. For example, there is a short breath break after almost every instance of “happy birthday”. These breath breaks register as rests in the notation of the performed durations. Portamentos in the sung melody are labeled with slurs in the third, sixth, and last bars. The tempo changes frequently, practically every time the voice re-enters following a breath break. The first “to you” pushes forward (*poco accel.*), the second “to you” holds back—the glissando arrives at the note before the “you” is vocalised, almost imperceptibly. In the next phrase, the octave leap builds to the climax, which is at a stately 60 bpm but accelerates to the end of “Mister President” before the final “happy birthday”.

The three examples above demonstrate how performed durations, both carefully sculpted ones and those due to chance, can be captured through transcription using conventional music notation. The following section extends this practice to the transcription of heart rhythms in ECG recordings of cardiac arrhythmias.

Abnormal Heart Rhythms

This section considers the transcription of arrhythmic heartbeats using conventional music notation. When the normal electrical activity in the heart is disrupted or altered, arrhythmia results and the heart can beat irregularly, or excessively fast or slow. The ECG recordings of a heart in sinus (normal) rhythm can make for decidedly uninteresting transcriptions, but the abnormal heart rhythms of arrhythmia are much more varied, offering the potential for producing highly musical rhythm transcriptions.

Take, for example, the trigeminy rhythm, an abnormal heart rhythm in which every third beat is a premature ventricular contraction (PVC). Each PVC is followed by a full compensatory pause (a skipped beat) because the heart is still in its refractory period and cannot respond to the electrical pulse for the next beat. PVCs tend to occur in

repeated patterns, aptly named bigeminy (every other beat), trigeminy (every third beat), quadrigeminy (every fourth beat), etc.

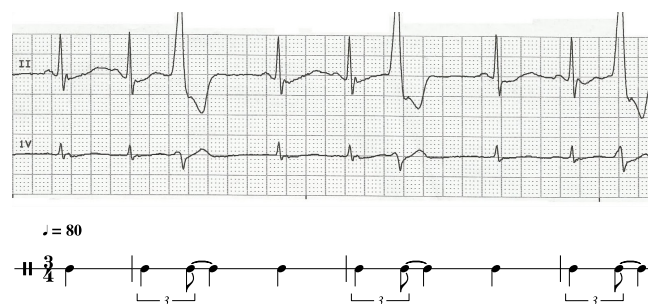


Figure 8. ECG* and transcription of a trigeminy rhythm.

Figure 8 shows a trigeminy rhythm and its transcription. One can imagine extensions to the other PVC rhythms such as the bigeminy and the quadrigeminy. Note the resemblance of the trigeminy rhythm—regular beat, early beat followed by a compensatory pause, regular beat—to a prototypical Viennese waltz rhythm. The onset of each beat is given by the peak, also known as the R of each QRS complex, in the signal of the upper graph. Given that the standard chart speed is 25 mm/s and a three-beat period is 56 mm on the chart, a beat is $(56/25)/3$ seconds long and the tempo is given by $60/((56/25)/3) \approx 80$ bpm. This demonstrates how the tempo is computed in the examples to follow. The RMSE between the R-R intervals and transcribed durations for Figure 8 is 24.8 ms; the details are shown in Table 4 and Figure 21 in the Appendix.

The next transcription examples are also derived from surface ECGs; they comprise of short summaries from a continuous 18-hour recording from a three-lead Holter monitor and show interesting states of AF.

Mixed Meters

Figure 9 shows the first ECG excerpt and the corresponding transcription of the rhythm. In this example, beats that are slightly more prominent (having greater voltage change) in the ECG are given tenuto-staccato articulation markings; R-R intervals that are slightly short of the full value of a beat duration are marked staccato and R-R intervals that are slightly longer than the full beat value are marked tenuto. The meter changes are assigned to group beats with similar morphology, such as the six wide complex beats in the middle of the sequence, and repeated rhythm patterns such as the 3 : 2 : 2 pattern. The RMSE between the R-R intervals in the ECG trace and the transcribed durations is 34.6 ms; the details are shown in Table 5 and Figure 22 in the Appendix.

The toggle between 7/8, subdivided as 3 : 2 : 2, and 5/8, subdivided as 3 : 2, meters is reminiscent of the third movement in Libby Larsen’s *Penta Metrics* (2004). The composer describes the piece as a buoyant dance built around the 7/8 pattern: three beamed eighth notes, eighth note +

*ECG of trigeminal premature ventricular contractions [Online image]. (2013). Retrieved April 16, 2017, from <http://floatnurse-mike.blogspot.com/2013/05/ekg-rhythm-strip-quiz-123.html>.

eighth note rest, eighth note + eighth note rest. Highlighted in the transcription are the patterns of three onsets separated by three-eighth-note and two-eighth note intervals that are part of the the $3 : 2 : x$ rhythmic motif. Note that the notation makes these patterns readily discernible.

Figure 10 shows the score of a short composition based (strictly) on the rhythm. It is made up of fragments cannibalized from Penta Metrics, movement III, sometimes transposed so as to fit with the local tonal context. For example, the first bar corresponds to the first bar of Penta Metrics III, the third bar corresponds to the second bar, and the ending chord is identical to that in Larsen's piece. In between, bars 2, 4, 5, and 6 are a mix of material, chords and descending octaves, from the sequences in bars 57-60 and bars 42-44, shown in Figures 11b and 11a, respectively.



(a) bars 42-44



(b) bars 57-60

Figure 11. Excerpts from Libby Larsen's *Penta Metrics*, movement III.

A video comparing the ECG and rhythm transcription, and the collaged “Mixed Meters” can be viewed at <https://vimeo.com/257248109>.

Siciliane

Figure 12 shows the second ECG excerpt and the corresponding transcription of the rhythm. For this example, the most prominent peak in the ECG sequence is highlighted with an accent on the corresponding note, and the wide complex beat with a tenuto mark; other ways to differentiate these waveform details are also possible. The notation in the middle section is simplified by invoking a metric modulation from 94 bpm to 126 bpm. This makes the new quarter note $3/4$ the value of the previous quarter note, a 25% reduction in time for a beat or a 33% increase in tempo or beat rate. A slight acceleration (marked *poco accel.*) indicates that the duration of the second beat in the penultimate bar is slightly shorter than the tempo might suggest; the acciaccatura tied to the final note prompts the early onset of the final note, achieving the effect of shortening the penultimate note. The changing meters are chosen to accommodate the different grouping structures. The RMSE between the R-R intervals in the ECG trace and the transcribed durations for Figure 12 is 53.0 ms; the details are given in Table 6 and Figure 23 in the Appendix.

This excerpt is slower than the first one, and the long half note in the second bar requires a melodic profile that will fit with this temporal structure. The melody that comes to mind is that of the “*Siciliane*” in Johann Sebastian Bach's

Flute Sonata No. 2 in E♭ major, BWV 1031, and the piece provides the material for the short composition shown in Figure 13. The original rhythm of the “*Siciliane*” is lyrical and straightforward, and close to the AF rhythm, but not the same. The melodic profile fits well the transcribed rhythm. Small adjustments are made to the melody so that it fits the rhythm. Figure 14 shows the original melody and the one that has been tweaked to fit the transcribed rhythm. The new melody uses bars 1, 2, and 4 of the original melody. A passing note was added in the third bar of the modified melody to fit the transcribed rhythm, and two notes from the last bar inserted to provide a bridge to the concluding bar.

An animation showing the correspondence between the ECG and the rhythm transcription, and between the modified “*Siciliane*” and the ECG can be viewed at <https://vimeo.com/221351463>.

Tango

Figure 15 shows the third and final ECG excerpt and the corresponding transcription of its rhythm. As before, the most prominent peaks in the ECG signal are assigned accent marks; the wide complex beats are given tenuto marks, as are notes of durations slightly longer than their notated values. The RMSE between the R-R intervals in the ECG trace and the transcribed durations is 40.1 ms; the details are given in Table 7 and Figure 24 in the Appendix.

Immediately apparent in the transcription are the $3 : 3 : 2$ rhythmic pattern characteristic of the tango, and variations on this pattern, $2 : 3 : x$. Capitalizing on the tango reference, the material for the short composition draws from a cadenza-like piano solo in Astor Piazzolla's “*Le Grand Tango*” for cello and piano (1982). The original excerpt from Piazzolla's piece that provided material for the short composition in Figure 16 is given in Figure 17. In the modified score, the third iteration of the descending sequence is reduced to fit the $7/8$ bar by removing the triplet figure. A bridge bar is inserted before material from the first and third bars are combined to reach the concluding bar, which also draws from material in the third bar but with a different finish.

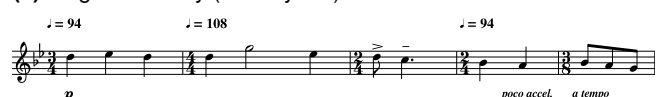
A video showing the ECG, rhythm transcription, and adapted “*Tango*” can be viewed at <https://vimeo.com/257253528>.

Conclusions and Discussions

Having traversed a variety of transcription examples ranging from the extreme rhythmic flexibility in performance to the natural floundering of sight reading (extreme in a different



(a) original melody (and rhythm)



(b) melody adjusted to fit the transcribed rhythm

Figure 14. Excerpt from Bach's “*Siciliane*” and its modification to fit the transcribed AF rhythm.

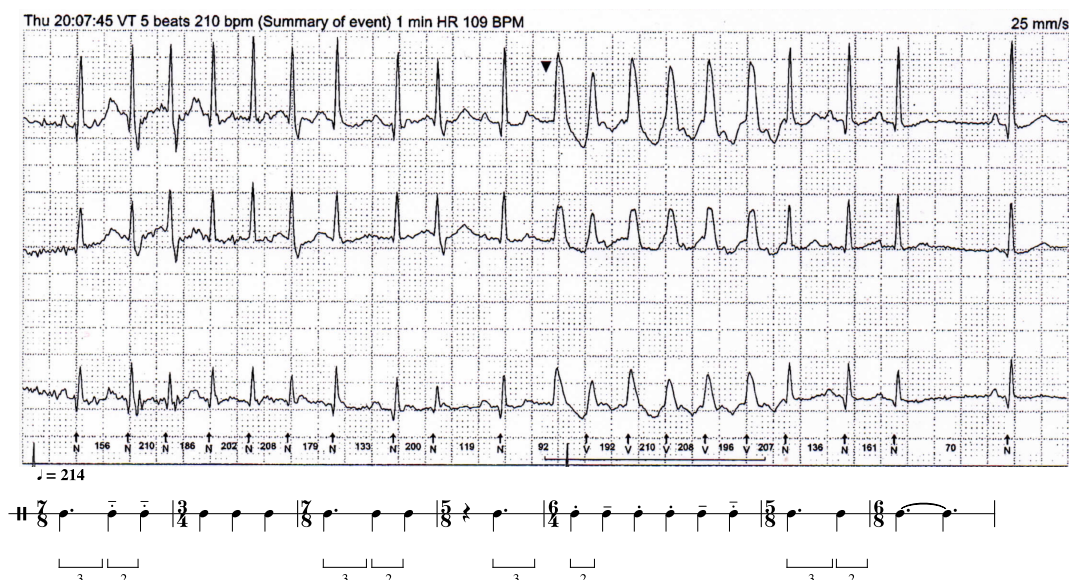


Figure 9. ECG and transcription of AF excerpt Thu 20-07-45 VT 5 beats 210 bpm (Summary of event) 1 min HR 109 BPM

Mixed Meters

Thu 20:07:45 VT 5 beats 210 bpm (Summary of event) 1 min HR 109 BPM

♩ = 214

Larsen-Chew (2017)



Figure 10. Composed fragment based on Thu 20-07-45 VT 5 beats 210 bpm (Summary of event) 1 min HR 109 BPM and Libby Larsen's *Penta Metrics*, movement III.



Figure 17. Excerpt from Piazzolla's "Le Grand Tango" used to fit the AF rhythm.

sense), to the dance-like rhythms of the premature ventricular contractions and atrial fibrillation, it is time to reflect on what

it means to be able to turn these rhythms accurately to music notation.

A symbolic representation can be used to encode knowledge that can serve as input to machine analysis of these time sequences, thus opening up new approaches for analyzing performed music and arrhythmia sequences. Further work needs to be done to gauge the stability of the transcriptions. Distance metrics can be devised to quantify distances between notations created by different transcribers for the same time sequence to determine consistency. Some key applications of the representation include large-scale deployment of motif detection, similarity assessment, and style classification. For example, after transforming heart period tachograms to elementary rhythm patterns, [Bettermann et al. \(1999\)](#) then used a hierarchical pattern scheme to compute the predominance and stability of rhythm pattern classes. Further analyses of the transcribed rhythms



Figure 12. ECG and transcription of AF excerpt Thu 16-52-59 Couplet 563ms (Summary of event) 1 min HR 83 BPM.

Siciliane

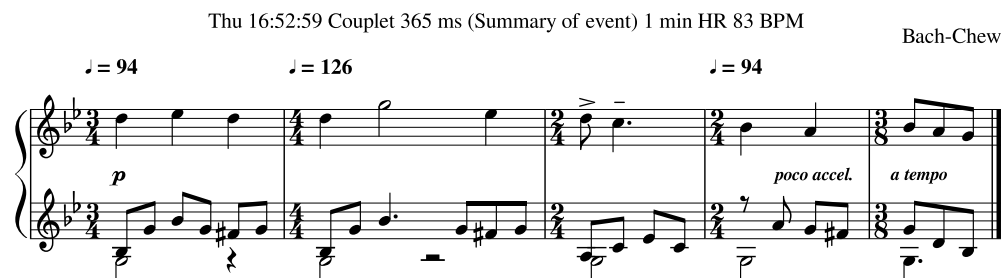


Figure 13. Composed fragment based on transcription of Thu 16-52-59 Couplet 563ms (Summary of event) 1 min HR 83 BPM and J. S. Bach's "Siciliane" from his *Flute Sonata No. 2 in E \flat major*, BWV 1031.



Figure 15. ECG and transcription of AF excerpt Thu 17-38-26 VT 4 beats 200 bpm (Summary of event) 1 min HR 105 BPM.

could reveal hierarchical structure, like that in [Lerdahl and Jackendoff \(1996\)](#).

The main challenge, for both music performance and cardiac arrhythmia, lies in determining what it is we wish to

Tango

Thu 17:38:26 VT 4 beats 200 bpm (Summary of event) 1 min HR 105 BPM

Piazzolla-Chew (2017)



Figure 16. Composed fragment based on transcription of Thu 17-38-26 VT 4 beats 200 bpm (Summary of event) 1 min HR 105 BPM and Astor Piazzolla's "Le Grand Tango".

represent. What are the essential structures of the information streams? What do they mean? Which of these structures are variable and subjective and which are fixed and invariant?

"Ideally, transcription should reveal the essential background structure of the temporal experience ... In that sense, transcription is a form of analysis in itself. The difficulty of transcribing free rhythm may result from the inadequate nature of the notational system but, at the same time, it signals a deeper analytical problem. Graphic signs can be easily invented once it is clear what we want to represent." Frigyesi (1993, p.60-62)

The changing meters, metric modulations, and detailed note groupings and subgroupings—for example, through the beaming of notes—call to question what can be notated but is not? What is notated and why? Which structures are the result of subjective interpretation and which are fundamental to the temporal sequence? The reality of the metrical groupings implied in each transcription needs to be further tested, for example, by comparing them to expert annotations. More features can be incorporated and larger numbers of transcriptions done to better understand the kinds of patterns that emerge. The transcriptions of abnormal heart rhythms can also serve as new sources of natural-sounding musical rhythms.

The transcriptions of the AF excerpts reveal the vast differences between the experience of the irregular heartbeats at different times of the day. "Mixed Meters" was recorded in the evening at 20:07:45, the "Siciliane" and the "Tango" in the late afternoon at 16:52:59 and 17:39:26, respectively. The rhythms differ not only in rate but also in rhythmic content. Conventional ways of describing AF as simply a condition with irregular heartbeats due to fibrillation in the upper (atrial) chambers of the heart fails to capture the

finer features of these time varying rhythmic structures. It may be that, like for musical styles, information encoded in these rhythmic patterns can be used to distinguish between different forms or phenotypic subtypes of AF, which may be helpful for disease stratification with impact on medical diagnostics and therapeutics.

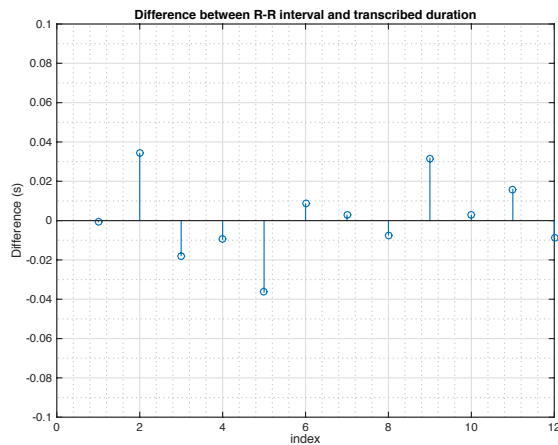
Appendix

Precision of Performed Music Transcriptions

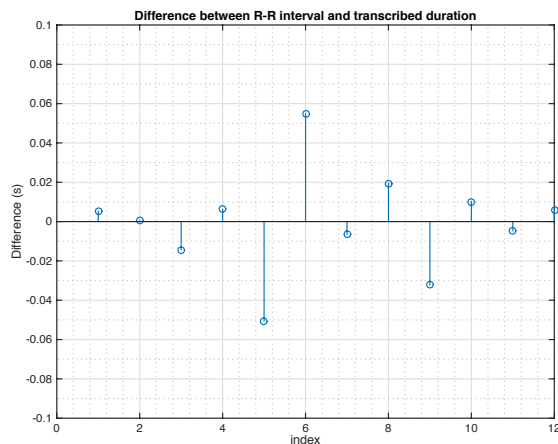
This section contains tables and graphs documenting the difference between the transcriptions and original rhythms derived from the recorded performances and ECGs. The differences are plotted as stem graphs and the tables provide the details of the RMSE calculations. Table 1 provides the numbers for the error calculations for Karajan's and Prêtre's recordings of "The Blue Danube", with the corresponding stem plots in Figure 18. Table 2 gives the numbers for Maria Callas' performance of "O Mio Babbino Caro", with the stem plot in Figure 19; and, Table 3 that for Marilyn Monroe's rendition of "Happy Birthday", with stem plot in Figure 20.

Precision of ECG Rhythm Transcriptions

This section contains tables and graphs documenting the difference between the R-R intervals derived from the ECG traces and the transcribed durations. The squared error between the two are given as well as the RMSE in the tables, and stem plots of the difference are given in the figures. Table 5 provides the numbers for the error calculations for the AF excerpt that formed the basis of "Mixed Meters", with the corresponding stem plot in Figure 22. Table 6 gives the numbers for the AF excerpt that became "Siciliane", with stem plot in Figure 22. And, Table 7 gives the numbers for the AF excerpt for the "Tango", with stem plot in Figure 24. Not reflected in the numbers and graphs are the effects



(a) Duration differences for performance conducted by Karajan



(b) Duration differences for performance conducted by Prêtre

Figure 18. Difference between performed and transcribed durations for “The Blue Danube” as performed by the Viennese Philharmonic Orchestra conducted by Herbert von Karajan (1987) and by Georges Prêtre (2010).

Karayan			Prêtre		
Perf dur	Trans dur	Sq diff	Perf dur	Trans dur	Sq diff
0.3599	0.3593	0.0000	0.5420	0.5474	0.0000
0.3251	0.3593	0.0012	0.4376	0.4380	0.0000
0.6502	0.6323	0.0003	0.6712	0.6569	0.0002
0.4586	0.4491	0.0001	0.4317	0.4380	0.0000
0.3019	0.2655	0.0013	0.3207	0.2703	0.0025
0.5224	0.5310	0.0001	0.7559	0.8108	0.0030
0.5283	0.5310	0.0000	0.5469	0.5405	0.0000
0.2728	0.2655	0.0001	0.3494	0.3689	0.0004
0.4992	0.5310	0.0010	0.5241	0.4918	0.0010
0.5283	0.5310	0.0000	0.4816	0.4918	0.0001
0.2496	0.2655	0.0003	0.3918	0.3871	0.0000
0.5399	0.5310	0.0001	0.5747	0.5806	0.0000
RMSE		0.0191	RMSE		0.0249

Table 1. Squared difference between performed and transcribed durations and RMSE (in seconds) for “The Blue Danube” as performed by the Viennese Philharmonic Orchestra conducted by Herbert von Karajan (1987) and by Georges Prêtre (2010).

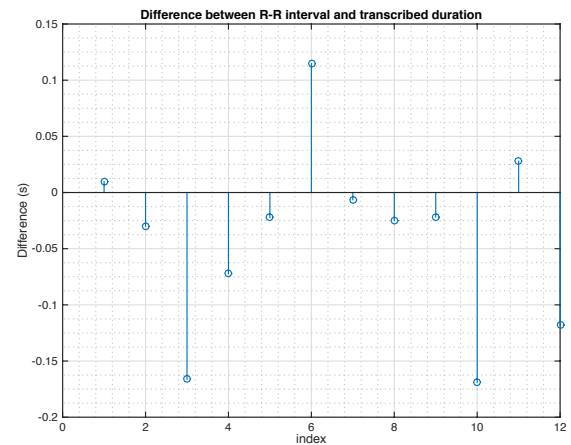


Figure 19. Difference between performed and transcribed durations for “O Mio Babbino” as performed by Maria Callas.

Performed duration (s)	Transcribed duration (s)	Squared difference (s ²)
0.6882	0.6977	0.0001
0.7276	0.6977	0.0009
0.8639	0.6977	0.0276
1.8164	1.7442	0.0052
2.1154	2.0930	0.0005
6.8620	6.9767	0.0132
1.0064	1.0000	0.0000
1.0249	1.0000	0.0006
1.0217	1.0000	0.0005
3.6688	3.5000	0.0285
2.9722	3.0000	0.0008
6.6177	6.5000	0.0139
RMSE		0.0874

Table 2. Squared difference between performed and transcribed durations and RMSE (in seconds) for “O Mio Babbino” as performed by Maria Callas.

of the accents and articulation markings incorporated in the transcriptions that mark amplitude (voltage) changes, waveform morphology, or slightly elongated or shortened durations.

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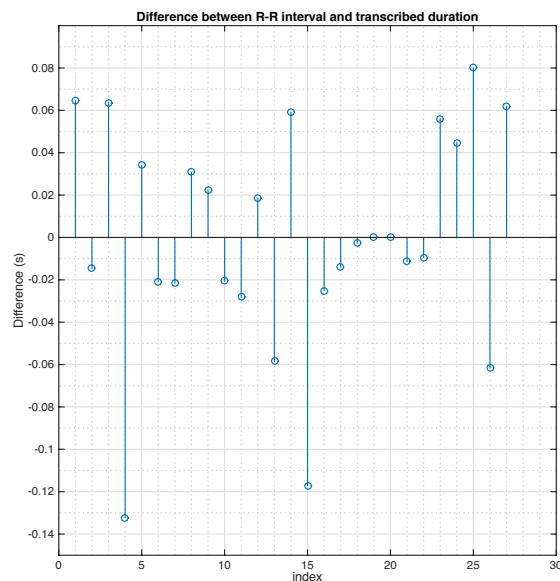


Figure 20. Difference between performed and transcribed durations for “Happy Birthday” as performed by Marilyn Monroe (1962).

Performed duration (s)	Transcribed duration (s)	Squared difference (s^2)
0.5355	0.6000	0.0042
1.2147	1.2000	0.0002
1.1363	1.2000	0.0041
1.3322	1.2000	0.0175
0.4833	0.5172	0.0012
2.0898	2.0690	0.0004
0.3918	0.3704	0.0005
0.3396	0.3704	0.0009
0.7184	0.7407	0.0005
1.5020	1.4815	0.0004
0.6531	0.6250	0.0008
2.4816	2.5000	0.0003
0.3918	0.3333	0.0034
0.2743	0.3333	0.0035
0.7837	0.6667	0.0137
1.3584	1.3333	0.0006
0.6139	0.6000	0.0002
0.4571	0.4545	0.0000
0.3657	0.3659	0.0000
0.1959	0.1961	0.0000
2.0114	2.0000	0.0001
0.5094	0.5000	0.0001
0.4441	0.5000	0.0031
0.7053	0.7500	0.0020
1.9200	2.0000	0.0064
0.5616	0.5000	0.0038
1.1882	1.2500	0.0038
RMSE		0.0515

Table 3. Squared difference between performed and transcribed durations and RMSE (in seconds) for “Happy Birthday” as performed by Marilyn Monroe (1962).

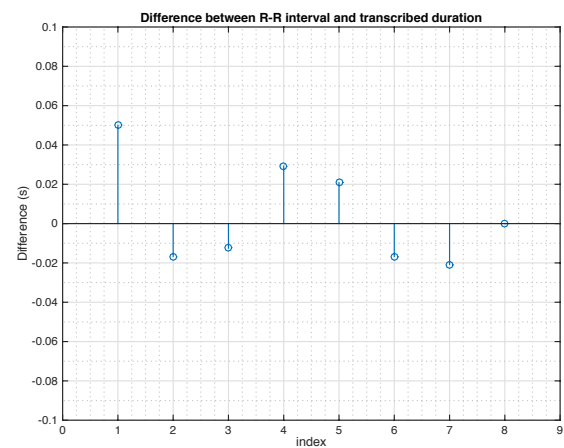


Figure 21. Difference between R-R intervals in ECG and transcribed durations for trigeminy example.

R-R interval (s)	Transcribed duration (s)	Squared difference (s^2)
0.7000	0.7500	0.0025
0.5167	0.5000	0.0003
1.0125	1.0000	0.0002
0.7208	0.7500	0.0009
0.4792	0.5000	0.0004
1.0167	1.0000	0.0003
0.7708	0.7500	0.0004
0.5000	0.5000	0.0000
RMSE		0.0248

Table 4. Squared difference between ECG and transcribed durations and RMSE (in seconds) for trigeminy example.

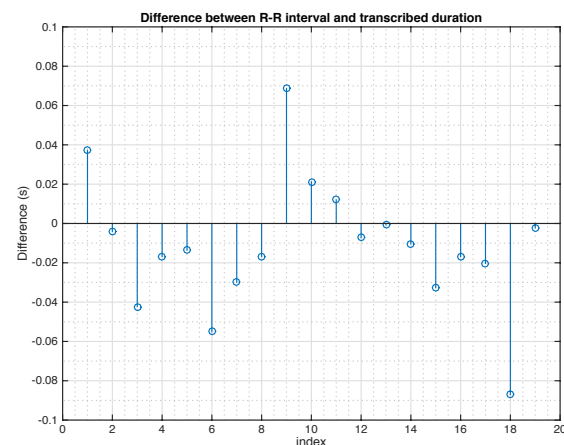


Figure 22. Difference between R-R intervals in ECG and transcribed durations for AF excerpt Thu 20-07-45 VT 5 beats 210 bpm (Summary of event) 1 min HR 109 BPM (“Mixed Meters”).

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R-R interval (s)	Transcribed duration (s)	Squared difference (s ²)
0.3834	0.4206	0.0014
0.2843	0.2804	0.0000
0.3227	0.2804	0.0018
0.2971	0.2804	0.0003
0.2939	0.2804	0.0002
0.3355	0.2804	0.0030
0.4505	0.4206	0.0009
0.2971	0.2804	0.0003
0.4920	0.5607	0.0047
0.3994	0.4206	0.0004
0.2684	0.2804	0.0001
0.2875	0.2804	0.0001
0.2812	0.2804	0.0000
0.2907	0.2804	0.0001
0.3131	0.2804	0.0011
0.2971	0.2804	0.0003
0.4409	0.4206	0.0004
0.3674	0.2804	0.0076
0.8435	0.8411	0.0000
RMSE		0.0346

Table 5. Squared difference between ECG and transcribed durations and RMSE (in seconds) for AF excerpt Thu 20-07-45 VT 5 beats 210 bpm (Summary of event) 1 min HR 109 BPM (“Mixed Meters”).

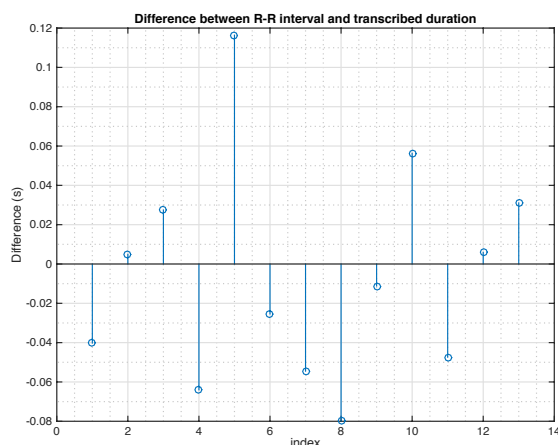


Figure 23. Difference between R-R intervals in ECG and transcribed durations for AF excerpt Thu 16-52-59 Couplet 563ms (Summary of event) 1 min HR 83 BPM (the “Siciliane”).

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R-R interval (s)	Transcribed duration (s)	Squared difference (s ²)
0.6785	0.6383	0.0016
0.6334	0.6383	0.0000
0.6109	0.6383	0.0007
0.5402	0.4762	0.0041
0.8360	0.9524	0.0135
0.5016	0.4762	0.0006
0.2926	0.2381	0.0030
0.7942	0.7143	0.0064
0.6495	0.6383	0.0001
0.5820	0.6383	0.0032
0.3666	0.3191	0.0022
0.2733	0.2793	0.0000
0.3280	0.3590	0.0010
RMSE		0.0530

Table 6. Squared difference between ECG and transcribed durations and RMSE (in seconds) for AF excerpt Thu 16-52-59 Couplet 563ms (Summary of event) 1 min HR 83 BPM (the “Siciliane”).

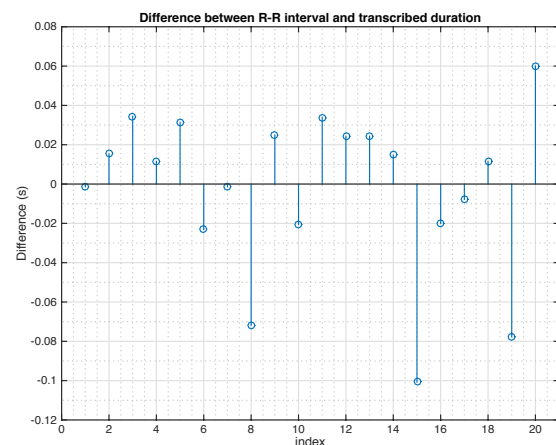


Figure 24. Difference between R-R intervals in ECG and transcribed durations for AF excerpt Thu 17-38-26 VT 4 beats 200 bpm (Summary of event) 1 min HR 105 BPM (the “Tango”).

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R-R interval (s)	Transcribed duration (s)	Squared difference (s ²)
0.3205	0.3191	0.0000
0.4647	0.4800	0.0002
0.4455	0.4800	0.0012
0.3077	0.3191	0.0001
0.4487	0.4800	0.0010
0.5032	0.4800	0.0005
0.3205	0.3191	0.0000
0.3910	0.3191	0.0052
0.4551	0.4800	0.0006
0.3397	0.3191	0.0004
0.2853	0.3191	0.0011
0.2949	0.3191	0.0006
0.2949	0.3191	0.0006
0.3045	0.3191	0.0002
0.4199	0.3191	0.0101
0.5000	0.4800	0.0004
0.3269	0.3191	0.0001
0.3077	0.3191	0.0001
0.5577	0.4800	0.0060
0.4199	0.4800	0.0036
	RMSE	0.0401

Table 7. Squared difference between R-R intervals in ECG and transcribed durations and RMSE (in seconds) for AF excerpt Thu 17-38-26 VT 4 beats 200 bpm (Summary of event) 1 min HR 105 BPM (the “Tango”).

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